

EVALUATING & GRAPHING PIECEWISE FUNCTIONS

A piecewise function is a function defined by two or more equations over a specified domain.

Given, $f(x) = \begin{cases} 3x - 4, & x < 0 \\ 3x + 1, & x \geq 0 \end{cases}$ If evaluating an x value less than 0, plug it into $3x - 4$, if evaluating an x value greater than or equal to zero, plug it into $3x + 1$.

Examples: Use the given functions to find the requested values

Given: $f(x) = \begin{cases} 3x - 4, & x < 0 \\ 3x + 1, & x \geq 0 \end{cases}$ and $g(x) = \begin{cases} x^2 + 1, & x < 2 \\ x - 1, & x \geq 2 \end{cases}$

- ① Look at the inequality to see where your x fits
- ② Plug in your x to that piece of the function only

1. a. $f(2)$ $2 \geq 0$ so
plug in 2 to
 $3x + 1$

$$3(-2) + 1 = 7$$

$$(2, 7)$$

b. $f(0)$ $0 \geq 0$ so
plug in 0 to
 $3x + 1$

$$3(0) + 1 = 1$$

c. $g(-6)$ $-6 > 2$ so plug
into $x^2 + 1$

$$(-6)^2 + 1
36 + 1 = 37$$

Graph the following piecewise functions **Make sure to pay close attention as to whether or not the dots should be open or closed!

5. $f(x) = \begin{cases} 2x + 3, & x \leq 1 \\ -x + 4, & x > 1 \end{cases}$

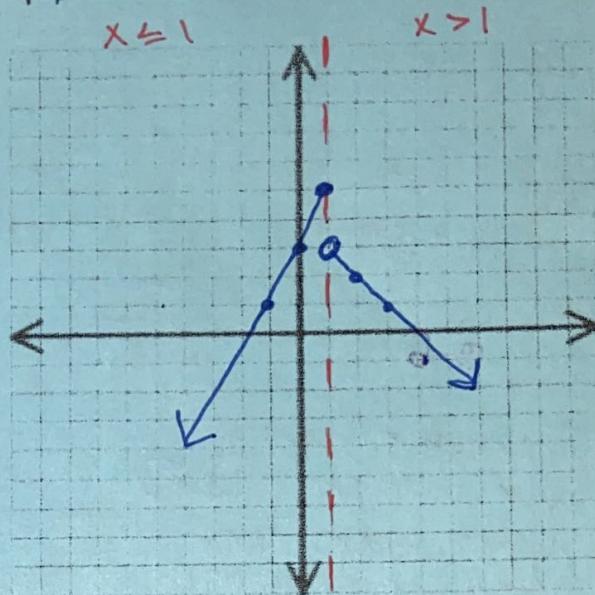
*critical pt.
draw a dashed
line through crit. pt.
+ don't cross*

$$y = 2x + 3$$

$x \leq 1$	$x y$
• 1	5
0	3
-1	1

$$y = -x + 4$$

$x > 1$	$x y$
open pt. so	1 3
2	2
3	1

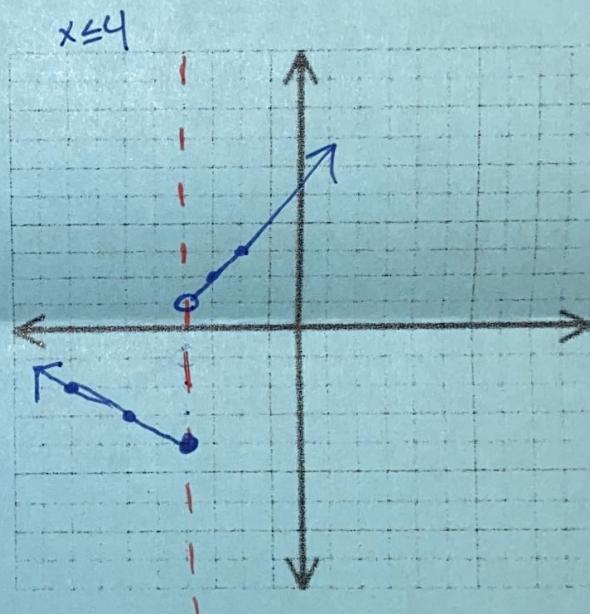


6. $g(x) = \begin{cases} -\frac{1}{2}x - 6, & x \leq -4 \\ x + 5, & x > -4 \end{cases}$

$$y = -\frac{1}{2}x - 6 \quad y = x + 5$$

<i>closed pt.</i>	$x y$
• -4	-4
-6	-3
-8	-2

<i>open pt.</i>	$x y$
-4	1
-3	2
-2	3



7. $h(x) = \begin{cases} x^2, & x \leq 0 \\ 3, & 0 < x \leq 2 \\ 2x - 1, & x > 2 \end{cases}$

$$y = x^2$$

$x \leq 0$	$x y$
• 0	0
-1	1
-2	4
-3	9

$$0 < x \leq 2$$

$x y$
0 3
1 3
2 3

$$y = 2x - 1$$

$x y$
0 3
1 5
2 7

