

Area of Oblique Triangles

p. 68

Area of a Triangle

**Given 2 Sides
& 1 Angle**

$$A = \frac{1}{2} a \cdot b \cdot \sin C$$

$$A = \frac{1}{2} a \cdot c \cdot \sin B$$

$$A = \frac{1}{2} b \cdot c \cdot \sin A$$

Area of a Triangle

**Given 3 Sides
(Heron's Formula)**

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{when } s = \frac{a+b+c}{2}$$

Given 2 sides & 1 angle:

1. Find the area of the Δ given $a=90$ m, $b=52$ m, & $C=102^\circ$.

$$\text{Area} = \frac{1}{2} ab \sin C$$

$$A = \frac{1}{2} (90)(52) \sin 102$$

$$A = 2,288.9 \text{ m}^2$$

2. Find the area of the Δ given $a=103$ cm, $c=58$ cm, & $B=74^\circ 30'$.

$$\text{Area} = \frac{1}{2} ac \sin B$$

$$A = .5(103)(58) \sin 74^\circ 30'$$

$$A = 2,878.4 \text{ cm}^2$$

3. Find the area of the Δ given $c=5.2$, $A=32^\circ$, & $B=78^\circ$.

$$\begin{array}{ll} a=2.9 & A=32 \\ b= & B=78 \\ c=5.2 & C=70 \end{array}$$

$$C=180-32-78$$

$$\frac{a}{\sin A} = \frac{c}{\sin C}$$

$$\frac{a}{\sin 32} = \frac{5.2}{\sin 70}$$

$$a = 2.9$$

$$\text{Area} = .5(a)(c)\sin B$$

$$A = .5(2.9)(5.2)\sin 78$$

$$A = 7.4 \text{ unit}^2$$

Given 3 sides use Heron's formula:

1. Find the area of the Δ given $a=9$, $b=3$, & $c=11$.

$$S = \frac{a+b+c}{2}$$

$$S = \frac{9+3+11}{2}$$

$$S = 11.5$$

$$\text{Area} = \sqrt{S(S-a)(S-b)(S-c)}$$

$$A = \sqrt{11.5(11.5-9)(11.5-3)(11.5-11)}$$

$$A = \sqrt{122.1875}$$

$$A = 11.1 \text{ u}^2$$

2. Find the area of the Δ given $a=6$, $b=8$, & $c=12$.

$$S = \frac{a+b+c}{2}$$

$$S = 13$$

$$A = \sqrt{S(S-a)(S-b)(S-c)}$$

$$A = \sqrt{455}$$

$$A = 21.3 \text{ u}^2$$

HW: p.298 #37-42 all