

# Transformations of Trig Functions

p.43

\*If you have a coefficient in front of  $x$  that is <sup>of  $\theta$</sup>  **INSIDE** the parenthesis factor it **OUT** 1st!

Example:  $f(x) = -3 \sin(2x - 5) + 1$

$f(x) = -3 \sin 2(x - 5/2) + 1$

$f(x) = a \text{ trig } b (x - c) + d$

$y = (-3) \sin 2(x - 5/2) + 1$     $y = -3 \sin 2(x - 5/2) + 1$     $y = -3 \sin 2(x - 5/2) + 1$     $y = -3 \sin 2(x - 5/2) + 1$

graph is reflected over x-axis + amp = 3 so that is the height above + below midline

per =  $\frac{2\pi}{b}$   
per =  $\frac{2\pi}{2}$   
per =  $\pi$  (horizontal shrink)

$c = 5/2$   
shift right  $5/2$

$d = 1$   
shift up 1

<ul style="list-style-type: none"> <li>a is the <b>amplitude</b> (height from midline)</li> <li>If a is <b>negative</b> then the graph reflects across the <b>X-axis</b>.</li> <li>If <math> a  &gt; 1</math>, then the graph has a vertical <b>stretch</b>.</li> <li>If a is a number between <b>0 + 1</b>, then the graph has a vertical <b>shrink</b>.</li> <li>ONLY <b>sin</b> and <b>cos</b> have amplitude.</li> <li>The sign is always <b>positive</b>!</li> </ul>	<ul style="list-style-type: none"> <li>b affects the <b>period length</b>.</li> <li>The period formula is <math>\frac{2\pi}{b}</math> for <b>sin, cos, csc, sec</b> or <math>\frac{\pi}{b}</math> for <b>tan + cot</b></li> <li>If <math>b &gt; 1</math>, then the graph has a horizontal <b>shrink</b></li> <li>If b is a number between <b>0 + 1</b> the graph has a horizontal <b>stretch</b></li> </ul>	<ul style="list-style-type: none"> <li>Be careful with the sign of c! It is always the <b>opposite sign</b> what you see in the equation.</li> <li>c is called the <b>Phase Shift</b>.</li> <li>It is your first point on the <b>left</b> of your graph</li> <li>If c is <b>positive</b> in the equation, then the graph moves <b>left</b></li> <li>If c is <b>negative</b> in the equation, then the graph moves <b>right</b></li> </ul>	<ul style="list-style-type: none"> <li>d is called the <b>vertical shift</b></li> <li>It is the new <b>midline</b> of your graph</li> <li>If d is <b>positive</b> in the equation, the graph moves <b>up</b></li> <li>If d is <b>negative</b> in the equation, the graph moves <b>down</b></li> </ul>
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