

### SLOPE OF THE TANGENT LINE

$$m_{tan} = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

This formula represents the **INSTANTANEOUS** rate of change

### DEFINITION OF A DERIVATIVE AT A POINT ( $a, f(a)$ )

$$f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

When to use this version:

-you are given a specific x value to evaluate the derivative at.

### DERIVATIVE

- Slope of a tangent line at  $x = a$
- Rate of change at  $x = a$
- Instantaneous rate of change or derivative
- Denoted by  $y'$ ,  $f'(x)$ , or  $\frac{dy}{dx}$

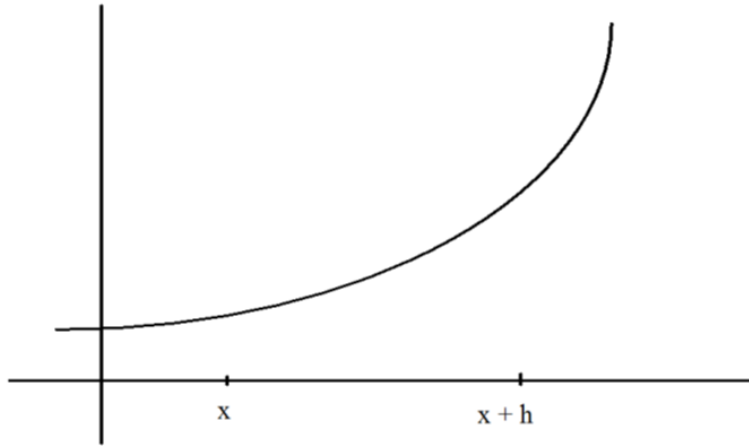
### TANGENT AND NORMAL EQUATIONS

To find the **tangent equation**:

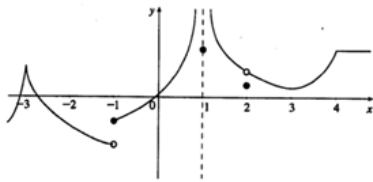
- find the slope of the tangent line (find the derivative)
- input the slope and the point into the point-slope form of a line (no need to simplify)

To find the equation of the **normal line**:

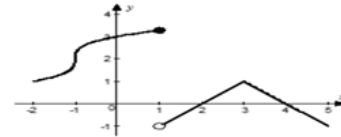
- Find the slope of the tangent line (find the derivative)
- Find the slope of the line perpendicular to the tangent line (negative reciprocal)
- Input the slope and the point into the point-slope form of a line (no need to simplify)



STATE THE X VALUES WHERE  $f$  IS NOT DIFFERENTIABLE AND THE REASON



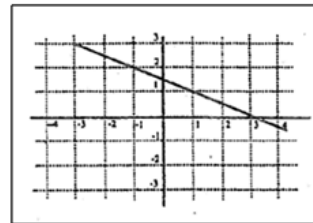
STATE THE X VALUES WHERE  $f$  IS NOT DIFFERENTIABLE AND THE REASON



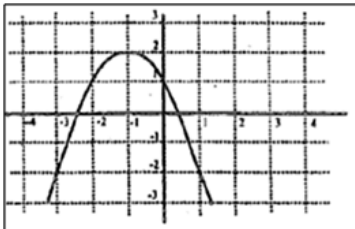
**RELATIONSHIP BETWEEN  $f, f', f''$**

$f$	$f'$	$f''$
-Cusp -Corner -Discontinuity -Removable -Infinite -jump -Vertical Tangent	DNE	DNE
Local max, local min (local extrema), horizontal tangent	0 On the x-axis	
$f$ increasing	Positive (Above the x-axis)	
$f$ decreasing	Negative (Below the x-axis)	
$f$ concave up	Increasing	Positive (Above the x-axis)
$f$ concave down	Decreasing	Negative (Below the x-axis)
Points of Inflections	Local Extrema	Change Signs

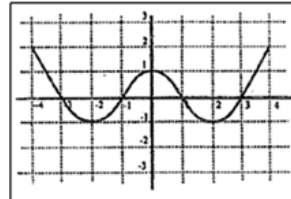
**1. GRAPH THE FIRST DERIVATIVE**



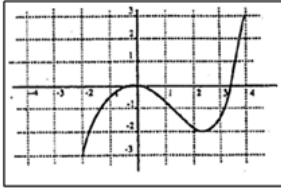
**2. GRAPH THE FIRST DERIVATIVE**



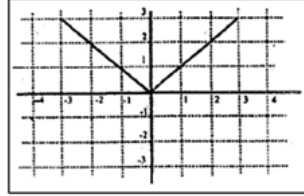
**3. GRAPH THE FIRST DERIVATIVE**



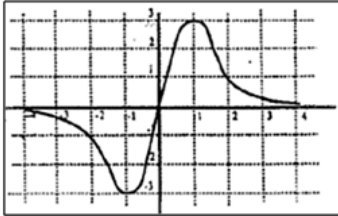
4. GRAPH THE FIRST DERIVATIVE



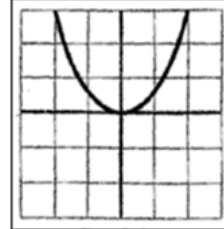
5. GRAPH THE FIRST DERIVATIVE



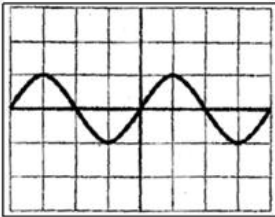
6. GRAPH THE FIRST DERIVATIVE

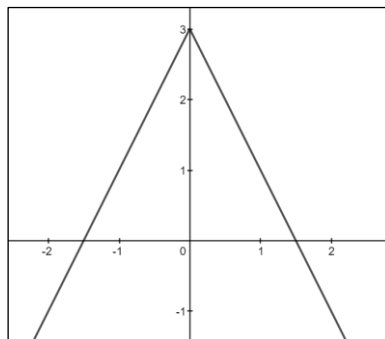
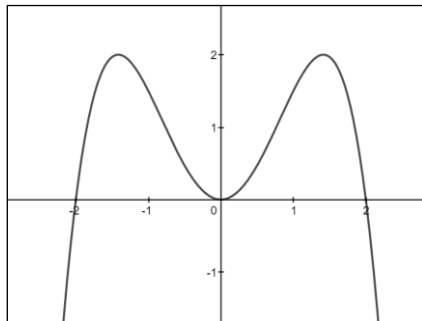
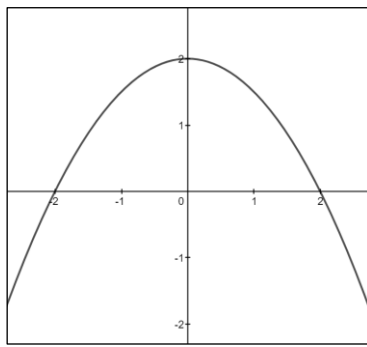
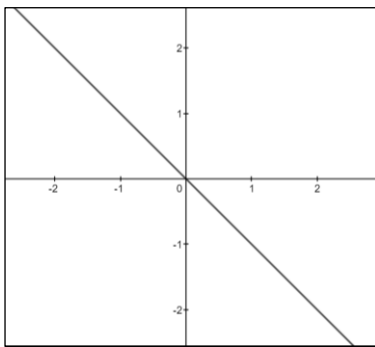


7. GRAPH THE  $F'(X)$  AND  $F''(X)$



8. GRAPH THE  $F'(X)$  AND  $F''(X)$





1. a.  $f(x)$  is continuous

b.  $f(3) = 2$

c.  $f'(x) > 0, (-\infty, 0) \cup (3, \infty)$

d.  $f'(x) < 0, (0, 3)$

e.  $f'(x) = 0$  at  $x = 0$  &  $x = 3$

4. a.  $f(x)$  has a jump disc. at  $x = -2$

b.  $f'(x) > 0, (-\infty, -2) \cup (-2, \infty)$

c.  $f''(x) < 0, (-\infty, -2)$

d.  $f''(x) > 0, (-2, \infty)$

2. a.  $f(x)$  is continuous

b.  $f'(x) < 0, (-\infty, 1)$

c.  $f'(x) > 0, (1, \infty)$

d.  $f'(x)$  is undefined at  $x = 1$

e.  $f''(x) < 0, (-\infty, 1) \cup (1, \infty)$

5. a.  $f(x)$  is continuous at  $[-4, 3]$

b.  $f'(x) < 0$  on  $(-4, -2)$

c.  $f'(x) > 0, (-2, 1) \cup (1, 3)$

d.  $f'(x)$  is undefined at  $x = -2$

e.  $f(-2) = -3$  and  $f(1) = 3$

f.  $f'(x) = 0$  at  $x = 1$

g.  $f''(x) < 0$ , on  $(-4, -2) \cup (-2, 1)$

h.  $f''(x) > 0$ , on  $(1, 3)$

3. a.  $f(x)$  is continuous

b.  $f'(x) < 0, (-\infty, 2) \cup (2, \infty)$

c.  $f'(x)$  is undefined at  $x = 2$

d.  $f''(x) < 0$  when  $x < 2$

e.  $f''(x) > 0$  when  $x > 2$

