

Characteristics of Polynomial Functions



Domain & Range

Domain and Range are written in interval notation.

Domain describes x-values

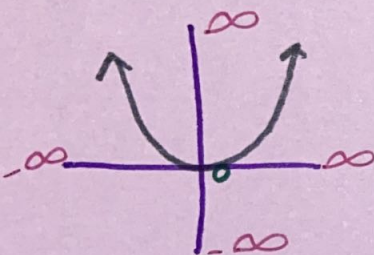
and range describes y-values

Domain: left, right Range: bottom, top

Use (or) when the # value is NOT included in the domain or range

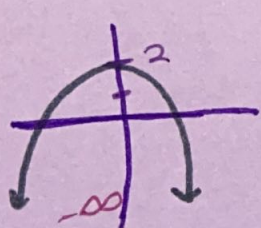
Use [or] when the # value IS included in the domain or range

Always use (or) with ∞ or $-\infty$



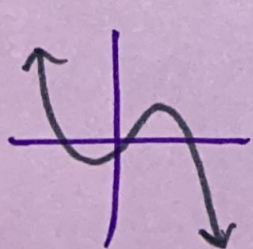
Domain: $(-\infty, \infty)$

Range: $[0, \infty)$



D: $(-\infty, \infty)$

R: $(-\infty, 2]$



D: $(-\infty, \infty)$

R: $(-\infty, \infty)$

Intercepts

X-intercepts are where the graph crosses or touches the x-axis

o Also called roots, zeros or solutions

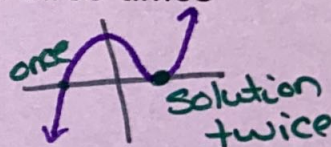
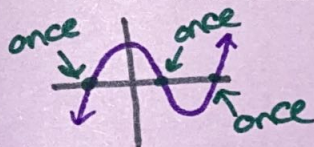
o Written as $(\#, 0)$

o To find algebraically, set function = 0 and solve for x

o If graph crosses the x-axis, that zero is a zero once

o If graph "bounces" off the x-axis, that zero is a zero twice

o If graph "wiggles" through the x-axis, that zero is a zero three times



Y-intercepts are where the graph crosses or touches the y-axis

o Written as $(0, \#)$

o To find algebraically, substitute 0 for x in function and simplify or it is just the constant

$$f(x) = x^3 - x^2 - 6x$$

X-intercepts ($y=0$)

$$0 = x^3 - x^2 - 6x \quad (0, 0)$$

$$0 = x(x^2 - x - 6) \quad (3, 0)$$

$$0 = x(x-3)(x+2) \quad (-2, 0)$$

$$\boxed{x=0} \quad x-3=0 \quad x+2=0$$

$$x=3 \quad x=-2$$

y-int. ($x=0$)

$$y = (0)^3 - (0)^2 - 6(0)$$

$$y = 0 \quad (0, 0)$$