

**Calculus : Derivative Applications**

**Group Work – Curve Sketching**

Name \_\_\_\_\_

Date \_\_\_\_\_ Period \_\_\_\_\_

Draw a possible graph of  $f(x)$  given the information below.

1. a.  $f(x)$  is continuous

$$f(x)$$

$$f(x)$$

b.  $f'(2) = 0$

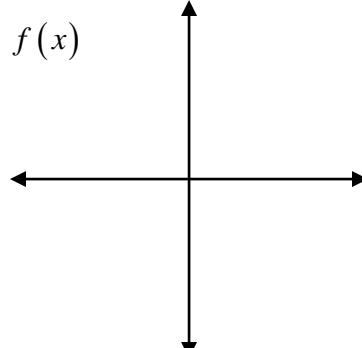
$$f'(x) \leftarrow \rightarrow$$

c.  $f'(x) > 0$ , if  $x < 2$

d.  $f'(x) < 0$ , if  $x > 2$

e.  $f''(x) < 0$  from  $(-\infty, \infty)$

$$f''(x) \leftarrow \rightarrow$$



2. a.  $f(x)$  is continuous

$$f(x)$$

$$f(x)$$

b.  $f'(x)$  does not exist at  $x = 1$

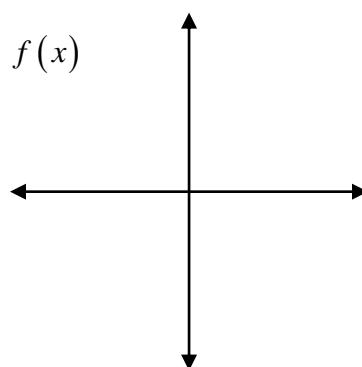
$$f'(x) \leftarrow \rightarrow$$

c.  $f''(x) < 0$  when  $x < 1$

d.  $f''(x) > 0$  when  $x > 1$

Draw two possibilities.

$$f''(x) \leftarrow \rightarrow$$



3. a.  $f(x)$  is continuous

$$f(x)$$

$$f(x)$$

b.  $f'(x) < 0$  when  $x < 1$

$$f'(x) \leftarrow \rightarrow$$

c.  $f'(x) > 0$  when  $x > 1$

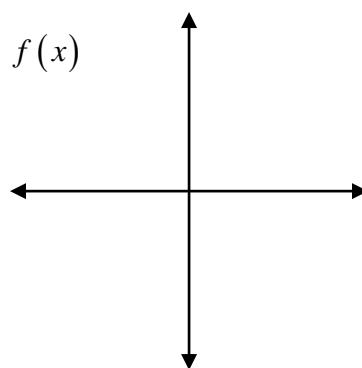
d.  $f''(x) > 0$  when  $x < 1$

e.  $f''(x) < 0$  when  $x > 1$

f.  $f'(x)$  does not exist at  $x = 1$

g.  $f''(x)$  does not exist at  $x = 1$

$$f''(x) \leftarrow \rightarrow$$

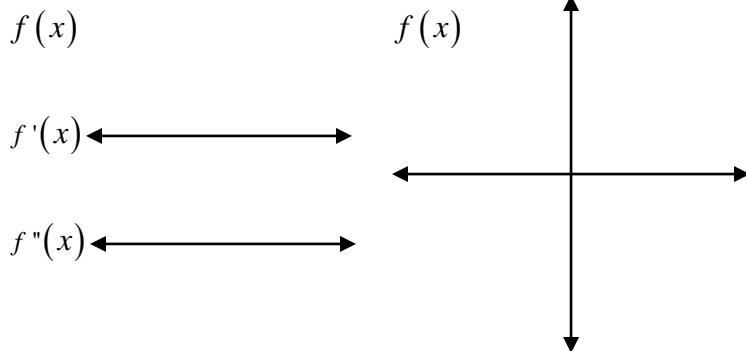


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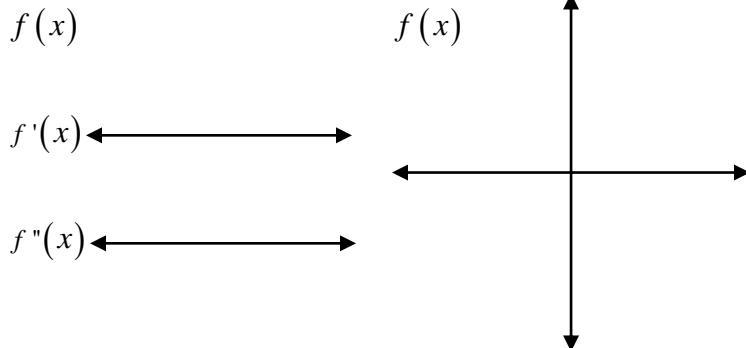
Name \_\_\_\_\_

Date \_\_\_\_\_ Period \_\_\_\_\_

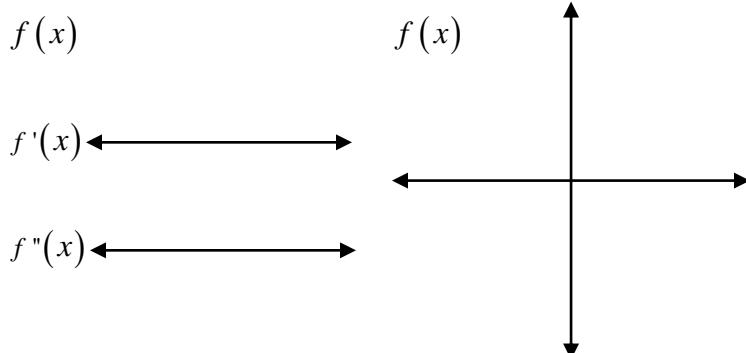
4. a.  $f(x)$  is continuous  
b.  $f'(x) < 0$  on  $(-1, 4)$   
c.  $f'(x) > 0$  on  $(-\infty, -1) \cup (4, \infty)$   
d.  $f'(x) = 0$  when  $x = -1, x = 4$   
e.  $f'' < 0$  on  $(-\infty, 1.5)$   
f.  $f'' > 0$  on  $(1.5, \infty)$



5. a.  $f(x)$  is continuous  
b.  $f'(x) > 0$  everywhere  
c.  $f'(x) = 0$  when  $x = -2, x = 3$   
d.  $f''(x) < 0$  on  $(-\infty, -2) \cup (1, 3)$   
e.  $f''(x) > 0$  on  $(-2, 1) \cup (3, \infty)$



6. a.  $f(x)$  is continuous  
b.  $f'(x) > 0$  when  $x < 2$   
c.  $f'(x) < 0$  when  $x > 2$   
d.  $f'(x)$  does not exist at  $x = 2$   
e.  $f''(x) > 0$  when  $x < 2$   
f.  $f''(x) < 0$  when  $x > 2$



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7. a.
- $f(x)$
- is not continuous at
- $x=3$
- $f(x)$

b.  $f'(x) > 0$  when  $x < 3$

c.  $f'(x) < 0$  when  $x > 3$

d.  $f''(x) > 0$  when  $x < 3$

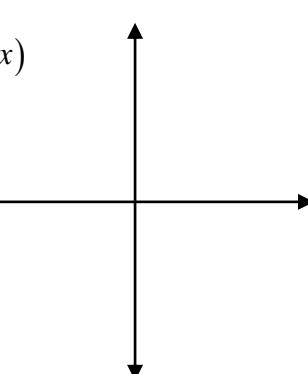
e.  $f''(x) > 0$  when  $x > 3$

f.  $f'(x)$  does not exist at  $x=3$

$f'(x) \leftarrow \longrightarrow$

$f''(x) \leftarrow \longrightarrow$

$f(x)$



8. a.
- $f(x)$
- is not continuous at
- $x=0$
- $f(x)$

b.  $f'(x)$  does not exist at  $x=0$

c.  $f'(x) > 0$  when  $x < 0$

$f'(x) \leftarrow \longrightarrow$

d.  $f'(x) > 0$  when  $x > 0$

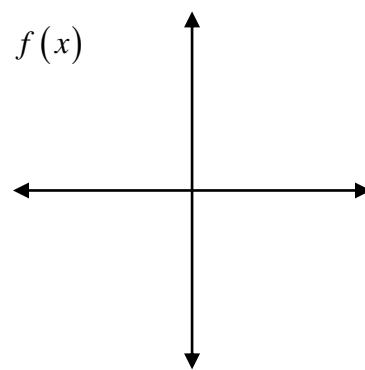
e.  $f''(x)$  does not exist at  $x=0$

$f''(x) \leftarrow \longrightarrow$

f.  $f''(x) > 0$  when  $x < 0$

g.  $f''(x) < 0$  when  $x > 0$

$f(x)$



9. a.
- $f(x)$
- is continuous
- $f(x)$

b.  $f(3)=0, f(1)=-2,$

$f(0)=-1, f(-1)=0$

$f'(x) \leftarrow \longrightarrow$

c.  $f'(x) > 0$  when  $1 < x < 3$

d.  $f'(x) < 0$  when  $x > 3$  or  $x < 1$

$f''(x) \leftarrow \longrightarrow$

e.  $f''(x) > 0$  when  $x < 0$  or  $1 < x < 3$

f.  $f''(x) < 0$  when  $0 < x < 1$  or  $x > 3$

$f(x)$

